

**PAPER III - COMPLEX ANALYSIS**

**Unit I**

Analytic functions as mappings: Elementary point set topology – Conformality – Linear transformations – Elementary conformal mappings.

**Unit II**

Complex Integration: Fundamental theorems – Cauchy's integral formula – Local properties of analytic functions – General form of Cauchy's theorem.

**Unit III**

Complex Integration: Calculus of residues – Harmonic functions

**Unit IV**

Series and Product Development: Power series expansion – Partial fractions and factorization – Entire functions – Riemann zeta function – Normal families.

**Unit V**

Riemann Mapping theorem – Elliptic functions: Simply periodic functions – Doubly periodic functions – the Weierstrass theory

**Text Books:**

1. L.V. Ahlfors, "Treatment as in Complex Analysis", III Edition, I.S.E., McGraw Hill.

Unit I : Chapter 3

Unit II : Chapter 4, Sections: 1, 2, 3 and 4

Unit III: Chapter 4, Sections 5 and 6

Unit IV: Chapter 5

Unit V : Chapter 6 – Section 1, Chapter 7

**Books for Reference :**

1. E.Hille, "analytic Functions", Vol.I and II.
2. J.B.Conway, "Functions of one Complex Variable".
3. Nevalinna and Paatro, "Complex analysis".